



Thermal pressure and thermal expansivity of solids at high temperatures

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ABSTRACT

Thermal pressure and thermal expansivity for sodium chloride and potassium chloride solids has been calculated at high temperatures using various Equation of State. The results from these calculations have been compared with the experimental data and the results are found to present close agreement with the experimental data. A close agreement between present study and the experiment data reveals the validity of the present work. The values of thermal pressure and thermal expansivity at high temperatures are useful to understand the thermo-elastic behavior of solids.

Keywords: Equation of State, Thermal expansivity, Thermal pressure

INTRODUCTION

Thermal pressure is a physical quantity of central importance¹ for investigating thermo-elastic properties of materials at high temperatures²⁻³. The volume expansion of solids is directly related to thermal pressure P_{th} due to rise in temperature⁴⁻⁵. The study of elastic properties is essential for examining and understanding of the dynamics of earth's deep interior, structure and composition of earth's lower mantle and in seismic studies.¹

The elasticity offers more information that the volume in interpreting the temperature dependence of equation of state (EOS) because the compressibility is defined by the derivative of volume⁶. The study of high pressure and high temperature behavior of solids demonstrate that the thermal expansivity (α) is a very important quantity needed for geophysical data analysis and condensed matter physics⁷⁻⁹, so various theoretical attempts have been made to solve this problem.

In order to understand the thermodynamic and thermo-elastic behavior of solids at high temperatures, it is necessary to have reliable values of elastic constants corresponding to such temperatures. The common methodology to determine the temperature dependence of

elastic constants is to use the volume expansion data for solids at high temperatures. In the present study, we calculated the thermal pressure and thermal expansivity for sodium chloride and potassium chloride.

THEORY

To calculate thermal pressure P_{th} , we are using these equations

$$\Delta P_{th} = K_0 \left(\frac{V}{V_0} - 1 \right) - \frac{1}{2} K_0 (K'_0 + 1) \left(\frac{V}{V_0} - 1 \right)^2 \quad (1)$$

$$\Delta P_{th} = \frac{K_0 \left(\frac{V}{V_0} - 1 \right) - \frac{1}{2} K_0 (K'_0 - 1) \left(\frac{V}{V_0} - 1 \right)^2}{\frac{V}{V_0}} \quad (2)$$

$$\Delta P_{th} = \frac{K_0 \left(\frac{V}{V_0} - 1 \right) - \frac{1}{2} K_0 (K'_0 - 3) \left(\frac{V}{V_0} - 1 \right)^2}{\left(\frac{V}{V_0} \right)^2} \quad (3)$$

Where K_0 and K'_0 are isothermal bulk modulus and its pressure derivatives both at $P = 0$ Equation (1) is derived by Shanker et al¹⁰, equation (2) has been obtained by Singh¹¹, equation (3) has been obtained by Shanker and Kushwah¹². Anderson gave one more relation for P_{th} using Anderson Grüneisen parameter

$$\Delta P_{th} = \frac{K_0}{M} \left[1 - \exp \left\{ - \delta_T^0 \left(\frac{V}{V_0} - 1 \right) \right\} \right] \quad (4)$$

Here the parameter M represents the slope of the plot between isothermal bulk modulus versus change in thermal pressure. Where δ_T^0 is the value of Anderson Grüneisen parameter δ_T at initial temperature. Thermal pressure evaluated through equation (4) based on the Anderson Grüneisen parameter is a volume dependent term^{13,14} can be considered more accurate and may be used to understand high temperature behavior of solids.

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One more equation, we are using for calculating thermal pressure using Kushwah logarithmic EOS¹⁵⁻¹⁶.

$$\Delta P_{th} = B_0 - B_1 \exp\left(-\frac{V/V_0}{B_2}\right) \quad (5)$$

Where B_0, B_1 and B_2 constant and their values are:

		B_0	B_1	B_2
For	NaCl	3.702	2471.01	0.1537
	KCl	2.591	1866.23	0.1519

For thermal expansivity, we are using these equations^{10, 17-19}

$$\frac{\Delta}{V_0} = \frac{V}{V_0} - 1 = \frac{1 - \left[1 - 2 \left(\frac{K'_0 + 1}{K_0}\right) P_{th}\right]^{\frac{1}{2}}}{(K'_0 + 1)} \quad (6)$$

The factor $(K'_0 + 1)$ in numerator if we replace it with $(K'_0 - 1)$ we get a new equation – Suzuki equation i.e

$$\frac{V}{V_0} - 1 = \frac{1 - \left[1 - 2 \left(\frac{K'_0 - 1}{K_0}\right) P_{th}\right]^{\frac{1}{2}}}{(K'_0 - 1)} \quad (7)$$

Recently Kumar²⁰ has shown that Suzuki relation²¹ as well as Tait¹⁸ and Murnaghan EOS¹⁹ can be used to obtain relation for thermal expansivity.

Tait EOS is expressed as:

$$\frac{V(0,T)}{V(0,T_R)} = [1 - A \alpha(0, T_R)(T - T_R)]^{\frac{1}{A}} \quad (8)$$

Murnaghan approach

$$\frac{V(0,T)}{V(0,T_R)} = [1 - (A - 1) \alpha(0, T_R)(T - T_R)]^{\frac{1}{A-1}} \quad (9)$$

RESULT AND DISCUSSION

Values of input parameters used in present calculation are given in table 1:^{1,22,23}

Solids	P_{th}				
	K_0	K'_0	K'_∞	M	δ_T^0
NaCl	24	5.38	3.23	5.96	5.78
KCl	17	5.46	3.28	5.91	5.71

Table 1. For Thermal expansivity ($T_R - 300K$)

T(K)	NaCl			KCl		
	α	$A(K_0)$	P_{th}	A	$A(K_0)$	P_{th}
	10^{-5}	GPa		10^{-5}	GPa	
	/K		/K			
300	11.8	24.0	0.00	11.0	17.0	0.00
350	12.2	23.2	0.14	11.3	16.4	0.09
400	12.7	22.4	1.28	11.7	15.9	0.19
450	13.2	21.6	0.43	12.1	15.4	0.28
500	13.7	20.8	0.57	12.6	14.7	0.37
550	14.3	19.9	0.71	13.2	14.2	0.47
600	14.8	19.0	0.85	13.7	13.7	0.56
650	15.4	18.1	0.99	14.2	13.2	0.65
700	16.0	17.3	1.13	14.7	12.6	0.75
750	16.6	16.5	1.27	15.2	12.0	0.84
800				15.7	11.5	0.93
850				16.2	10.9	1.02

Table 2. Thermal Pressure for NaCl computed from (a) equation (1), (b) equation (2), (c) equation (3), (d) equation (4), (e) equation (5) and (f) experimental data¹

T(K)	V/V_0	ΔP_{th}					
		(a)	(b)	(c)	(d)	(e)	(f)
300	1.0000	0.00	0.00	0.00	0.00	0.00	0.00
350	1.0060	0.14	0.14	0.14	0.14	0.15	0.14
400	1.0123	0.28	0.28	0.28	0.28	0.29	0.28
450	1.0188	0.42	0.42	0.42	0.41	0.44	0.43
500	1.0256	0.56	0.55	0.57	0.55	0.58	0.57
550	1.0328	0.70	0.68	0.71	0.70	0.72	0.71
600	1.0402	0.84	0.81	0.85	0.83	0.86	0.85
650	1.0480	0.98	0.93	0.99	0.98	1.00	0.99
700	1.0561	1.11	1.04	1.13	1.12	1.13	1.13
750	1.0645	1.23	1.15	1.23	1.25	1.28	1.27
800	1.0732	1.35	1.25	1.39	1.39	1.41	1.41
850	1.0832	1.46	1.35	1.52	1.52	1.54	1.54
900	1.0916	1.56	1.43	1.64	1.66	1.67	1.67
950	1.1012	1.64	1.49	1.76	1.78	1.79	1.79
1000	1.1112	1.72	1.55	1.88	1.90	1.91	1.91
1050	1.1214	1.79	1.59	1.98	2.03	2.03	2.03
1100	1.1319	1.83	1.62	2.08	2.14	2.13	2.13
1150	1.1427	1.87	1.63	2.18	2.26	2.24	2.24
1200	1.1538	1.88	1.62	2.27	2.27	2.35	2.35

Thermal Pressure for KCl computed from (a) equation (1), (b) equation (2), (c) equation (3), (d) equation (4), (e) equation (5) and (f) experimental data¹

T(K)	V/V_0	ΔP_{th}					
		(a)	(b)	(c)	(d)	(e)	(f)
300	1.0000	0.00	0.00	0.00	0.00	0.00	0.00
350	1.0054	0.09	0.09	0.09	0.09	0.09	0.09
400	1.0112	0.18	0.18	0.18	0.18	0.19	0.19
450	1.0172	0.28	0.27	0.28	0.27	0.28	0.28
500	1.0235	0.37	0.36	0.37	0.36	0.37	0.37
550	1.0301	0.46	0.45	0.46	0.45	0.47	0.47
600	1.0370	0.55	0.53	0.55	0.55	0.56	0.56
650	1.0442	0.64	0.62	0.65	0.64	0.66	0.65
700	1.0517	0.73	0.70	0.74	0.73	0.75	0.75
750	1.0594	0.82	0.77	0.83	0.83	0.84	0.84
800	1.0675	0.90	0.84	0.92	0.92	0.93	0.93
850	1.0759	0.97	0.90	1.01	1.01	1.02	1.02
900	1.0847	1.05	0.96	1.10	1.10	1.11	1.11
950	1.0938	1.11	1.02	1.18	1.19	1.19	1.19
1000	1.1032	1.17	1.06	1.26	1.28	1.28	1.28
1050	1.1129	1.21	1.10	1.33	1.37	1.36	1.36
1100	1.1230	1.26	1.12	1.41	1.45	1.44	1.44
1150	1.1334	1.29	1.14	1.48	1.53	1.51	1.51
1200	1.1437	1.31	1.14	1.54	1.61	1.59	1.59

Table 3. Thermal expansivity V/V_0 for sodium chloride and potassium chloride (a) calculated from equation (6), (b) calculated from equation (7) due to Suzuki, (c) calculated

from equation (8) Tait Approach, (d) calculated from equation (9) Murnaghan Approach and (e) based on experimental data¹.

NaCl					
T(K)	(a)	(b)	(c)	(d)	(e)
300	1.0000	1.0000	1.0000	1.0000	1.0000
350	1.0059	1.0059	1.0066	1.0066	1.0060
400	1.0121	1.0120	1.0151	1.0149	1.0123
450	1.0191	1.0187	1.0262	1.0258	1.0188
500	1.0259	1.0251	1.0414	1.0403	1.0256
550	1.0331	1.0318	1.0644	1.0614	1.0328
600	1.0407	1.0387	1.1026	1.0933	1.0402
650	1.0489	1.0459	1.2277	1.1606	1.0480
700	1.0577	1.0533			1.0561
750	1.0674	1.0611			1.0645

KCl					
T(K)	(a)	(b)	(c)	(d)	(e)
300	1.0000	1.0000	1.0000	1.0000	1.0000
350	1.0054	1.0054	1.0060	1.0060	1.0054
400	1.0116	1.0115	1.0130	1.0129	1.0112
450	1.0175	1.0171	1.0215	1.0213	1.0172
500	1.0236	1.0230	1.0320	1.0314	1.0235
550	1.0307	1.0296	1.0455	1.0442	1.0301
600	1.0375	1.0358	1.0623	1.0598	1.0370
650	1.0447	1.0422	1.0842	1.0794	1.0442
700	1.0533	1.0496	1.1131	1.1039	1.0517
750	1.0617	1.0565	1.1540	1.1353	1.0594
800	1.0710	1.0638	1.2246	1.1801	1.0675
850	1.0814	1.0714	1.3846	1.2410	1.0759

The above calculations for thermal pressure and thermal expansivity for NaCl and KCl have been shown by the various graphs as follows:

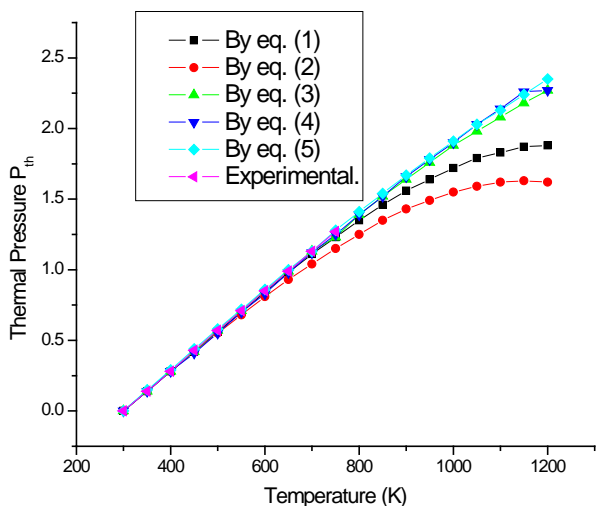


Figure 1. Thermal Pressure (P_{th}) versus Temperature (K) for NaCl.

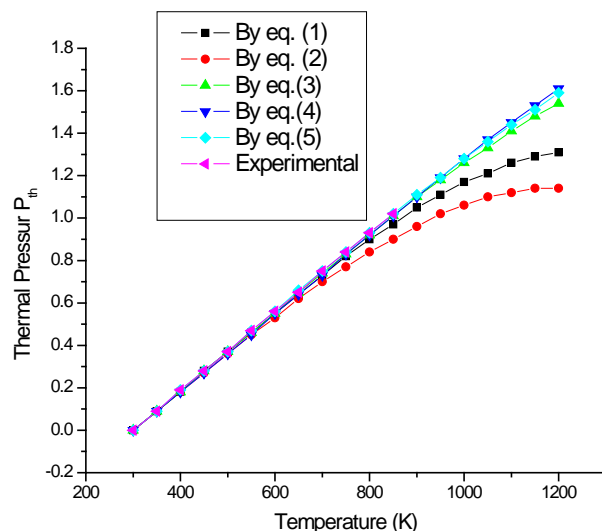


Figure 2. Thermal Pressure (P_{th}) versus Temperature (K) for KCl.

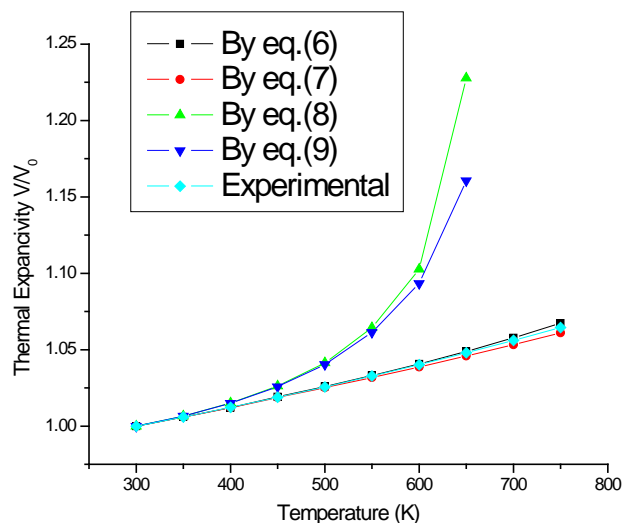


Figure 3. Thermal Expansivity (V/V_0) versus Temperature (K) for NaCl.

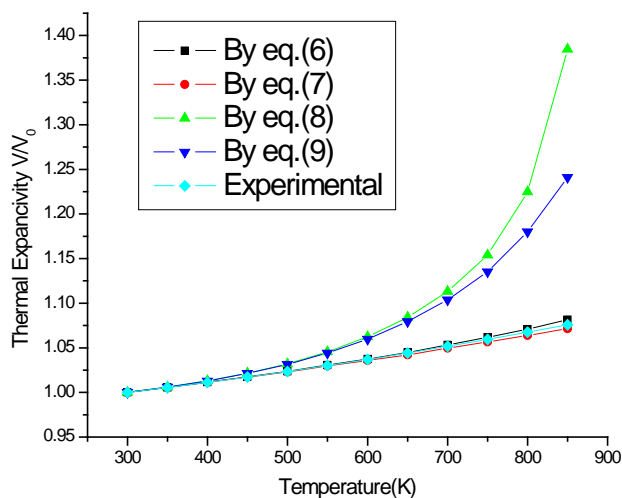


Figure 4. Thermal Expansivity (V/V_0) versus Temperature (K) for KCl.

CONCLUSION

In conclusion, the results calculated for thermal pressure and thermal expansivity agree with experimental data for Sodium chloride and Potassium Chloride but in case of thermal pressure, the results calculated by eq. 2 deviates above the temperature 550 K and in case of thermal expansivity, the results calculated by Tait and Murnaghan Approach does not agree well with experimental data.

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